

## Optimum seat design for the quadruple offset butterfly valve by analysis of variance with orthogonal array

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**Abstract:** In onshore and offshore plant engineering, a broad use of pipe system have been achieved and accordingly related technologies has been developed especially in the field of flow control valves. The aim of this study is to suggest the quadruple offset butterfly valve for bi-directional applications which show equivalent operating torque characteristics of the triple offset butterfly valve. Seat design parameters for the quadruple offset butterfly valve are determined by the proposed method utilizing both ANOVA (analysis of variance) and the orthogonal array. Through additive model considering the effect of design parameters on seating torque, mean estimation is performed and thus its optimization results are verified by design of experiment results. The insight obtained from the present study is beneficial for valve design engineers to develop reliable and integrated design of the quadruple offset butterfly valve.

**Keywords:** Butterfly Valve, Quadruple Offset, Analysis of Variance (ANOVA), Orthogonal Array, Optimization

### 1. Introduction

With advancement of industrialization, facilities in industries are likely to diversify and become more complex. Accordingly, offshore and onshore plant industries tend to focus on not only improving productivities together with reducing production costs but also maintaining and managing the uniformity of products through enhancing energy efficiencies and simplifying processes with automatic control between components.

Offshore and onshore plants are aimed at manufacturing products as inter-connected systems with a variety of control loops. In order to ensure the quality of the products, each control loop must work for limiting the main drivers including pressure, flow, water level, temperature, etc. within the allowable range of each parameter [1]. Equipment and devices installed in plants should be provided various sources including material, energy, and information enabling them efficiently. In this regard, pipelines play an important role to deliver material and energy from one device to another and the control of their function is mainly dependent on the valve system. Furthermore, it is found that they are essential components transporting various fluids in ships although pipelines are relatively small compared with the cooling system built in onshore plants such as desalination plants, chemical plants, nuclear and thermal power plants.

Recently, the design requirements related to temperature,

pressure, and flow rate, etc. are likely to become more and more severe due to the trend of larger plants and production facilities. At present, either of a globe valve or gate valve is widely spread for control high-pressure. According to the previous researcher [2][3], the number of applications of both butterfly and ball valves are expected to gradually continue to rise due to the issues such as high cost and low maintainability of these valves.

Until now, numerical studies related to the butterfly valve were mainly conducted for examining their performance including the loss coefficient of the valve, torque characteristics, flow control characteristics and the structural reliabilities [4][5]. With respect to the concentrated butterfly valve, the characteristics of the valve is numerically assessed based on the structural and flow analysis in order to ensure the structural reliability and the flow stability and therefore an optimum design of the valve disc was performed by the orthogonal array [5][6]. Further, the study of the pressure drop and cavitation characteristics was carried out for the concentrated butterfly-type valve [7]. For the offset butterfly valve, Park et al. [8] focused on the effect of the eccentric shaft on the internal flow characteristics and Lee et al. [9] analyzed the flow characteristics with varying shape of the seat.

For the studies associated with butterfly valves, since they were designed in accordance with ANSI B 16.34 Class

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150–300 which was designed for low-pressure. It is hard to find track records in the high-pressure which causes severe structural deformation to the disc, detachment of the seat and non-applicability of the reverse direction. In this regards, Lee and Kim [10] proposed the quadruple offset butterfly valve which is keeping advantages of triple offset butterfly valve with improving reversal performance and identified sensitivities of each parameter based on the parametric studies in order to ensure the applicability under high-pressure.

The purpose of this study is to define design range of the main parameters for the seat and to optimize the shape of the seat in association with seating torque of the quadruple offset butterfly valve which is capable of applying bi-directional applications. By applying ANOVA and orthogonal array for the seat optimization, sensitivities for design parameter are identified and compared with the results of mean estimation. The mean estimation of seating torque is evaluated by the additive model considering the main effects of each design parameter and validated by comparison with the analysis results.

## 2. Quadruple Offset Butterfly Valve

The butterfly valve can be divided into two types in aspect of operating axis. Concentric type and offset type whether the disc aligns with rotating axis depending on the structure of the seat. There are two offset valves are mostly used which named as double and triple eccentric offset butterfly valve. According to the structure of offset in the valve, the operating torque characteristic is significantly varies according to the flow induced pressure differences between upstream and downstream of the pipeline. However, for valves under operating conditions, seating torque required to open the closed valve disc separating from the seat is the most important factors affecting the valve performance and its effect on the disc becomes more significant when it is fully closed. Therefore, the most important factor in design of a driving part of valves is to diminish seating torque acting on the seat itself. As a result, a variety of seat configurations has been proposed in terms of reducing seating torque.

Figure 1 describes a comparison example of the seating torque ratio for double and triple offset butterfly valves in terms of disc opening angles. It is observed that seating torque of triple offset valves in low opening angles varies more dramatically than the double offset valves due to the effect of the changing contact type from a surface to a line [11]. However, it has been recognized that the triple offset butterfly valve shows weak performance for the reverse direction because of the applied contact type which is only able to seal the leakage

by line type.

Figure 2 shows schematic representation of the triple offset butterfly valve. Using the triple offset butterfly valve in reverse direction, when the engagement angle is large, the leakage is more likely to happen, and on the other hand, when the angle is relatively small, the durability of seat could drop due to the significant increment in torque. To tackle these issues, Lee and Kim [10] proposed the new quadruple offset butterfly valve applying offset for the seat as shown in Figure 3. According to their results, it was expected to improve the valve performance in reverse direction with keeping the benefits of the triple offset valve.

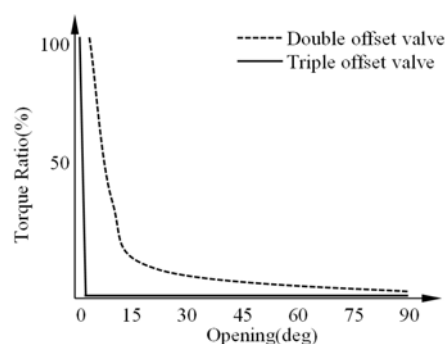


Figure 1: Seating torque characteristics of butterfly valve

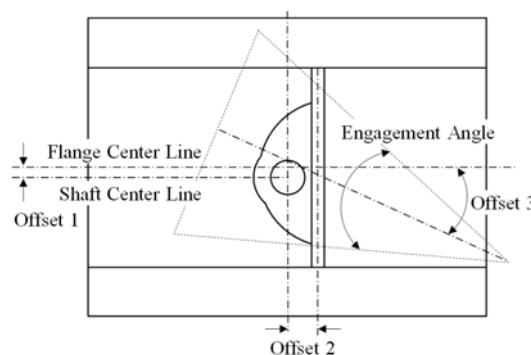


Figure 2: Triple offset butterfly valve

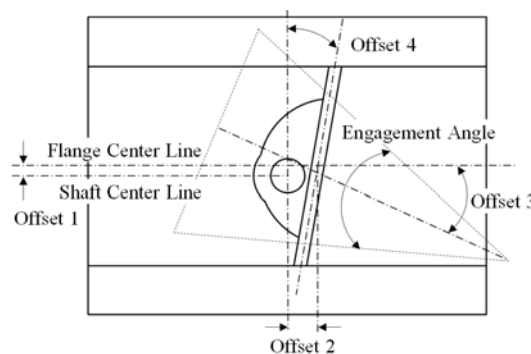


Figure 3: Quadruple offset butterfly valve

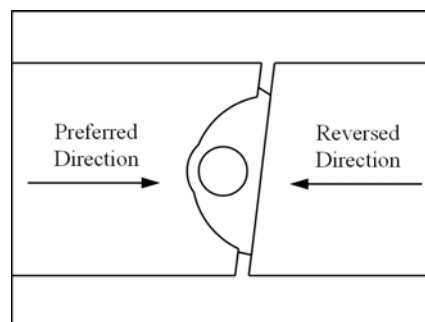
### 3. Optimization Algorithm

In the present study, the optimization algorithm is developed based on the structural analysis, the orthogonal array and ANOVA, and the detail of each step is as follows:

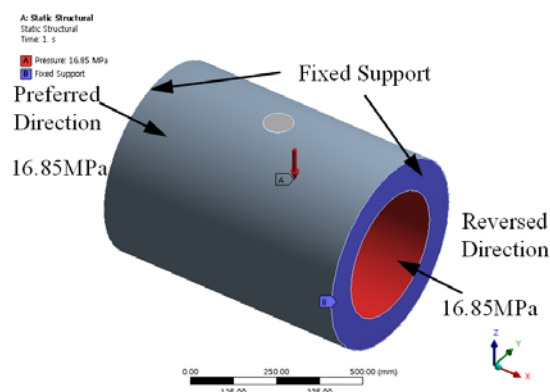
- Step 1. Definition and selection of object values
- Step 2. Determine design parameters, the number of level and their values
- Step 3. Selection of orthogonal array and allocation of design parameters considering overall degrees
- Step 4. Executing design of experiment and calculating object values according to the combinations of design parameters determined by the orthogonal array
- Step 5. Calculating mean of object values for each level of design parameters
- Step 6. Selection of significant factors influencing most on the object values based on the results of ANOVA
- Step 7. Determining optimum design conditions resulting from the mean estimation
- Step 8. Estimation of the object values for significant factors under optimum design conditions by additive model
- Step 9. Implementing confirmation experiment and estimating real object values under optimum design conditions
- Step 10. Determining optimum design conditions as an optimum solution based on the validation of additivity
- Step 11. If the additivity of the additive model is not met for the criteria, back to the Step 4 in consideration of developing new orthogonal array of selection of the design parameters, adjusting the level range and including the interaction term and perform all the steps accordingly.

### 4. Optimization Seat Configuration

The aim of this chapter is to analyze the relation between each design parameter and seating torque for the quadruple offset butterfly valve. By using finite element method computation, torque of the shaft is numerically calculated in terms of rotational directions, here preferred and reverse directions. In the present study, the fluid flow from left to right is defined as the preferred direction as shown in **Figure 4**. Applied boundary conditions of the finite element method computation are shown in **Figure 5**. It is assumed that both ends of valves are fixed and the load, 16.85 MPa is applied for the inside of Class 900. To apply the contact condition between the disc and the body of the seat, “No separation” contact condition is applied. The “Bond” contact condition is applied for the valve body and the disc with their stems.



**Figure 4:** Valve operating direction



**Figure 5:** Boundary condition for experiment

#### 4.1 Determining design parameters

In the present study, 5 design parameters for the quadruple offset butterfly valve are defined as shown in **Figure 6**. The detail is as follows.

- Parameter 1: Offset between flange and shaft center lines (fixed at 10.0mm)
- Parameter 2: Offset between seat and shaft center lines (fixed at 47.5 mm)
- Parameter 3: Offset between flange center line and seat angle
- Parameter 4: Angle offset between shaft center line and seat center line
- Parameter 5: Engagement angle of seat

The configuration optimization is carried out for parameters 3, 4 and 5.

Park [12] noted that in order to identify linear and nonlinear effect, level 2 and 3 of the design parameter are proper, respectively. In the present study, level 3 is applied. **Table 1** represents the level of each design parameter based on the determined results along with the maximum and minimum ranges at which no physical interference. To analyze interactions among parameters, 3 design parameters with 3-level by using the orthogonal array of full factorial experiment are defined and summarized in **Table 1**. **Table 2** shows the numerical

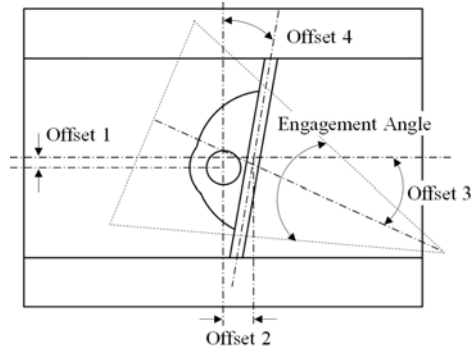


Figure 6: Quadruple offset butterfly valve design parameters

Table 1: Design parameters and levels

Design Parameter			Level		
Symbol	Description	Unit	1	2	3
A	Offset 3	deg.	12	15	18
B	Offset 4	deg.	1	4	7
C	Engagement angle	deg.	8	14	20

Table 2: Orthogonal array design and the experimental results

Run	A	B	C	Response (kN·m)	
				Preferred Direction	Reverse Direction
1	1	1	1	11.06	10.76
2			2	10.22	9.91
3			3	9.55	9.32
4		2	1	11.04	10.65
5			2	10.1	9.72
6			3	9.37	9.09
7		3	1	11.04	10.56
8			2	10	9.52
9			3	9.21	8.88
10	2	1	1	10.69	10.43
11			2	9.91	9.66
12			3	9.3	9.11
13		2	1	10.64	10.32
14			2	9.79	9.49
15			3	9.13	8.91
16		3	1	10.62	10.21
17			2	9.68	9.31
18			3	8.98	8.72
19	3	1	1	10.27	10.05
20			2	9.56	9.36
21			3	9	8.86
22		2	1	10.21	9.94
23			2	9.44	9.2
24			3	8.84	8.67
25		3	1	10.17	9.83
26			2	9.34	9.04
27			3	8.7	8.51

results of in accordance with the design parameters determined by the orthogonal array of full factorial experiment.

#### 4.2 Analysis of variance (ANOVA)

ANOVA results for torque in terms of the level average are presented in Table 3. It is found that the maximum difference ( $\Delta$ ) between average levels in mean estimation shows C, A and B order.

Figure 7 summarizes the mean response in terms of parameter levels. It is observed that the slope according to the level change as depicted in Table 3 is relatively large in design parameter C which shows the most influential design parameter on the seating torque. In order to analyze the significant factors in seating torque, ANOVA is implemented and the results are presented in Table 4 and Table 5 in terms of design parameters. As a result, design parameter C shows the most significant factor from the  $F$  value and contribution ratio of parameters. Figure 8 displays the level of contribution among design parameters. Figure 9 shows the results of interaction effect between design parameters and it shows that effect is insignificant.

Table 3: Mean effect response table

Level	Preferred Direction			Reverse Direction		
	A	B	C	A	B	C
1	10.178	9.953	10.638	9.824	9.717	10.305
2	9.860	9.839	9.783	9.572	9.554	9.468
3	9.504	9.750	9.121	9.273	9.398	8.896
$\Delta$	0.673	0.202	1.518	0.551	0.319	1.409
Rank	2	3	1	2	3	1

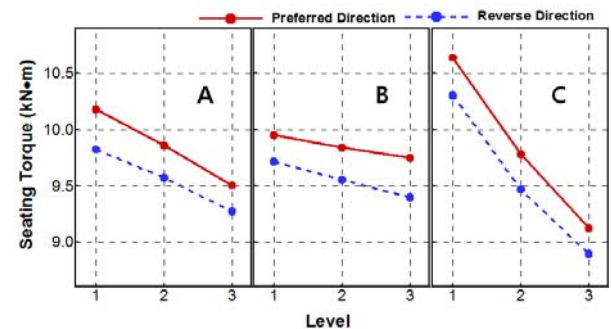


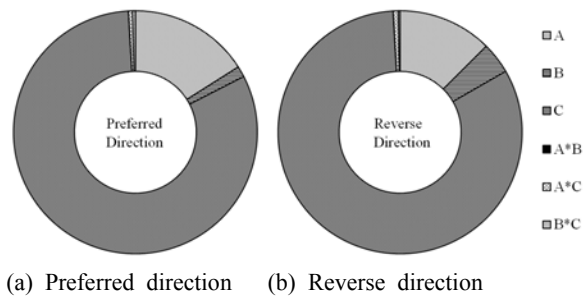
Figure 7: Mean effect response graph

Table 4: ANOVA results table for preferred direction

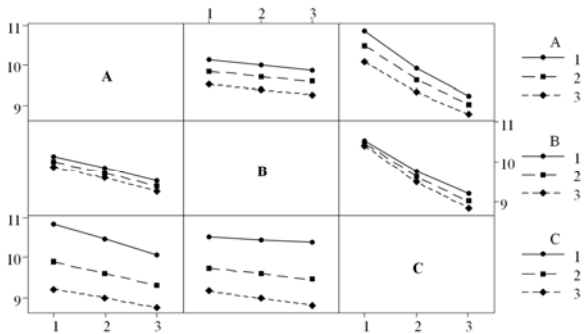
Source	DOF	SS	MS	F value	Percentage of contribution (%)
A	2	2.0425	1.0212	4000.35	15.99
B	2	0.1851	0.0925	362.51	1.45
C	2	10.4246	5.2123	20417.55	81.64
A×B	4	0.0003	0.0001	0.26	0
A×C	4	0.0670	0.0168	65.64	0.52
B×C	4	0.0501	0.0125	49.04	0.39
Error	8	0.0020	0.0003		
Total	26	12.7695			100.0

**Table 5:** ANOVA results table for reverse direction

Source	DOF	SS	MS	F value	Percentage of contribution (%)
A	2	1.3699	0.6849	2348.15	12.49
B	2	0.4574	0.2287	784.05	4.17
C	2	9.0384	4.5192	15493.26	82.42
A×B	4	0.0015	0.0004	1.29	0.01
A×C	4	0.0721	0.0180	61.79	0.66
B×C	4	0.0269	0.0067	23.09	0.25
Error	8	0.0023	0.0003		
Total	26	10.9662			100.0



**Figure 8:** Contribution of factors



**Figure 9:** Interaction Plot

**Table 6:** ANOVA results for preferred direction : without interaction effect

Source	DOF	SS	MS	F value
A	2	2.0425	2.0425	1.0212
B	2	0.1851	0.1851	0.0925
C	2	10.4246	10.4246	5.2123
Error	20	0.1194	0.1194	0.006
Total	26	12.7715		

**Table 7:** ANOVA results for reverse direction : without interaction effect

Source	DOF	SS	MS	F value
A	2	1.3699	1.3699	0.6849
B	2	0.4574	0.4574	0.2287
C	2	9.0384	9.0384	4.5192
Error	20	0.1029	0.1029	0.0051
Total	26	10.9685		

### 4.3 Determining optimum design parameters

Since the optimum conditions of significant factors minimizing seating torque is a combinations of both ends, according to the results of mean estimate, the design parameters of A, B and C with 3-level, would be the optimum conditions. To apply for the additive model, ANOVA is conducted for design parameters of A, B, and C without interaction effect by the orthogonal array. The results are presented in **Table 6** and **Table 7**. Mean estimation of seating torque within optimum design conditions is predicted by additive model using **Equation (1)** considering main effects of significant factors.

$$\hat{\mu} = \mu + \sum_{i=1}^N (\bar{\mu}_i - \mu) \quad (1)$$

Where,  $\mu$  is the mean of in **Table 2** represents the results of measured seating torque for experiment simulations in terms of directions. And  $N$  is number of design parameters and  $\bar{\mu}_i$  is the mean of torque in the optimum condition for  $i^{\text{th}}$  design parameter. Selected optimum design condition is the same as "Run 27" of the orthogonal array. The additivity of additive model is validated by the seating difference between prediction and experiment. The prediction is estimated based on the 95% of confidence interval of the population mean. The population mean is calculated by **Equation (2)**, it is confirmed that the difference, is within the error limit [13].

$$\beta = t\left(\phi_e, \frac{\alpha}{2}\right) \sqrt{\frac{MS_e}{m}} \quad (2)$$

$$\frac{1}{m} = \sum_{i=1}^N \frac{1}{N_i} - 2 \times \frac{1}{N_T} \quad (3)$$

Where  $\phi_e$  is degree of error,  $\alpha$  is confidence coefficient (1 - confidence interval),  $MS_e$  is variance of error and  $m$  is significant number variation. And  $N_i$  is number of experiment data in each parameter and  $N_T$  is number of total experiment data.

### 4.4 Results of Optimum seat design

For alternative of selected model, it is unable to implement for seat interaction in practical cases. In order to settle down this problem, the engagement angle is adjusted and therefore the interaction effect is eliminated. **Table 8** summarizes the selected optimum design conditions. Under selected conditions, mean estimation of the seating torque using additive model are developed by a form of prediction equation suggested **Equation (1)**. **Table 2** shows the mean of measured seating

torque,  $\mu$  in experiment simulation for each direction.  $\bar{C}_{25\text{deg}}$  represents the prediction values at 25 degrees resulting from the 2nd order regression analysis for mean estimation of design parameter,  $C$  in **Table 3**.

**Table 8:** Optimum values of design parameters

Design Parameter	Unit	Value
Offset 1	mm	47.5
Offset 2	mm	10.0
Offset 3	deg.	18.0
Offset 4	deg.	7.0
Engagement Angle	deg.	25.0

A validation experiment is implemented according to the final optimum design conditions and their results are 8.924 kN·m for preferred direction and 8.182 kN·m for reverse direction. **Table 9** summarizes the experimental results of optimum seat design. Seating torque shows reduction in 4.7% for preferred direction and in 3.9 % for reverse direction compared to the optimal design. Furthermore, the additivity of applied additive model in optimal model prediction is verified by using not only the difference of seating torque between the estimated and actual torque at optimum design conditions but also the 95% confidence interval. The difference of seating torque between the estimated and the actual torque for both directions is proved within the error limit of the population mean calculated from the **Equation (2)** and **Equation (3)**.

**Table 9:** Experimental results of optimum seat design

Condition	Item	Response (kN·m)	
		Preferred Direction	Reverse Direction
$A_3B_3C_3$ (Run 27)	Experiment	8.704	8.511
	Estimation	8.680	8.455
	$\delta$ ( $ Exp. - Est. $ )	0.024	0.056
	Error limit ( $\beta$ )	0.082	0.076
Optimum values	Experiment	8.294	8.182
	Estimation	8.293	8.192
	$\delta$ ( $ Exp. - Est. $ )	0.001	0.010
	Error limit ( $\beta$ )	0.082	0.076
Remark	Experiment	- 4.7%	- 3.9%
	Estimation	- 4.5%	- 3.1%

## 5. Conclusion

The aim of this study is to define design range of the main parameters for seat and to optimize the shape of the seat in association with seating torque of quadruple offset butterfly valve capable of bi-directional applications.

Based on the results obtained from the present study, the following conclusions can be drawn.

1. Design parameters for the quadruple offset butterfly valve are identified by orthogonal array and ANOVA and therefore it is observed that the engagement angle is the most influential parameter. Further, it is noted that the interaction effect among design parameters for representing the shape of the seat are negligible.
2. Using optimization algorithm utilizing orthogonal array and ANOVA, optimization of seat configuration for the quadruple offset butterfly valve is carried out. As a result, the design parameter without interference is determined and the reduction of seating torque is found 4.7 % and 3.9% in preferred and reverse directions, respectively.
3. At present study, the optimization is only taking into account the seating torque as an objective function. However, it is necessary to consider the hydrodynamic torque. In near future, to establish the validity of the proposed method, the actual product will be manufactured and tested.

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