



[ICACE2022] Model identification of two double-acting pistons pump

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Abstract: The Covid-19 pandemic has had a comprehensive and far-reaching impact on various fields, especially in the medical aspect. Additionally, many variants of this coronavirus have appeared due to mutation, each of which has distinguished influences. During the Covid-19 pandemic, medical equipment, especially ventilators, has seen a severe shortage. Thus, many studies of ventilators machine have been carried out around the world. And according to these studies, airflow control is one of the critical issues of ventilator machine research that saves human life. Understanding the above problem, it is necessary to conduct system modeling and obtain a model which has high linearity so that the parameters of the ventilation can be controlled to achieve better accuracy. This paper presents the model identification of a two double-acting piston pump system using experimental data. First order plus dead time method is applied to achieve the identification model. The data used for identification and validation are collected by conducting several practical tests on the two double-acting pistons pump system. The discussion on the identified model and future works are also included in this paper.

Keywords: Covid-19, Medical ventilator, Two double-acting pistons pump, First order plus dead time, Model identification.

1. Introduction

The Covid-19 pandemic which appeared as an outbreak in Wuhan (China) in 2019 [1]-[6] has spread over the world and led to devastating consequences not only for insanity but also for economy, society, and people's lives. This pandemic has caused crisis and paralysis in the medical system in every country that suffers from the outbreak of Covid-19, even the most developed nation is no exception. On the health-care aspect, the Covid-19 affects directly to the human respiratory system, especially those who have underlying medical conditions. Thus, the demand for medical ventilators in general and simple ventilators in specific rises quickly [7] as a consequence to assist patients with respiration [8]. During this period, myriad types of medical ventilators are designed and manufactured with different principles; some of which use the CAM mechanism [9], and others use pneumatics [10] or bag valve mask ventilators [11]. Another breed of the medical ventilator is also used widely as a simple ventilator [12].

This type of ventilator helps to resolve problems associated with the need for ventilators such as inter-and intrahospital transport [13], protocolized weaning from ventilation [14], or patients in a persistent vegetative state (PVS).

In general, a medical ventilator consists of two important main components, the air compressor, and the control unit. Among these two main units, the air compressor has more effects on the operating principles of the ventilator. Beside the mentioned mechanisms above, the air compressor using a piston mechanism, especially a double-acting pistons, gives excellent performance through time [15]. This kind of air compressor gives the advantage to generate a consistent airflow during the piston's cycle, therefore, there is no idle time in the control process. In addition, the double-acting pistons mechanism has the ability to operate smoothly with nearly zero noise and high stability, thus, its application is widely spread and prioritized in designing medical ventilators. The second component of the medical ventilator is

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the control unit. In present ventilators, various control units are studied and applied, some typical control units are adaptive neuro-fuzzy control [16], and model-free control [17]. The application of a specific control unit on the ventilator system requires a model that describes the dynamic behavior of the system accurately. This paper presents a model identification of two double-acting pistons pump (DAPP) [18][19]. The first order plus dead time (FOPDT) model is used for this identification process.

The contents of this paper are organized as follows: Section 2 describes the overall system of the DAPP used in the ventilator. Then, the model identification process by applying the FOPDT model is presented in Section 3. After that, Section 4 provides experimental tests along with results and discussion. At the end of this paper, conclusions and future work is mentioned in Section 5.

2. Overall system description

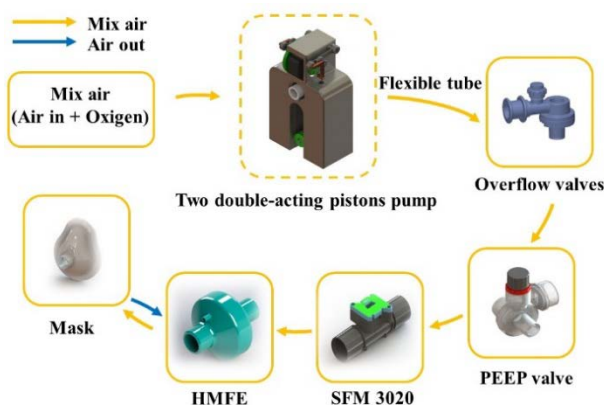


Figure 1: Operation process of two double-acting pistons pump system

Figure 1 describes the operation process of DAPP system. In which, the DAPP is driven by a brushless direct current (BLDC) motor. The flexible tube that is responsible for air transmission between each part of the system is made of medical specialized silicon. The DAPP also uses two types of exhausting valves. The first type is the overflow valve. The overflow valve gives the ability for the DAPP system to exhaust the air when the pressure in the system increases above the limit pressure. This helps to protect the system from being damaged. The other exhausting valve is the positive end-expiratory pressure (PEEP) valve, which is used for maintaining the residual pressure existing in the patient’s lung at the end of the expiration phase. This PEEP valve plays an important role in assisting patient’s breath and avoiding

collapsed lungs which has the possibility of augmenting the mortality rate of patients [20]-[23]. Besides these exhausting valves, a mass flow sensor SFM 3020 manufactured by SENSIRON is included in the system with the purpose of retrieving airflow data on the outlet. The pumped mixed air must be filtered by a heat moisture exchanger filter (HMEF) before entering patient’s respiratory system. The HMEF contributes to humidification, warming-inspired air. It also helps to capture airborne particles and prevent bacteria or viruses from flowing into the patient. Additionally, the usage of the HMEF can help to isolate the contaminated airflow from the patient to the DAPP system during the exhalation.

3. Model identification

Upon present literature in the model identification and control field, the FOPDT model still receives considerable attraction due to its simplicity and well performance in fitting many industrial processes. A FOPDT model can be written as follow:

$$\tau_p \dot{y}(t) = -y(t) + K_p u(t - \theta_p) \quad (1)$$

where τ_p is the time constant; $y(t)$ is the response signal of the system; K_p is the process gain or the steady state gain; $u(t)$ is the input signal of the system and θ_p is the dead time. By calculating three parameters τ_p, K_p, θ_p based on the sample data, the DAPP system can be identified in form of an estimated FOPDT model. Numerous methods were studied and applied in determining or approximating these parameters [24]-[27]. Among them, there is a class of methods that use the step response of the system to estimate the FOPDT model. Typically, the graphical method and area method was introduced by document [28] to estimate FOPDT model based on the step response. The two-points method [29] is also a simple one for this application. However, all three mentioned methods were sensitive with noise, and a novel method was proposed in the document [30] in which the least-squares method was applied to calculate the parameters of the FOPDT model.

In this paper, the graphical method is adopted for model identification of the DAPP system because of the simplicity of the method and the low-noise characteristic of the DAPP. According to this method, the parameters τ_p, K_p, θ_p are identified based on the step response of the DAPP system. Let’s define u_{ss}, y_{ss} respectively as the steady state input and the output signal of the system. Assume that two separated steady-state output signals

y_{ss1}, y_{ss2} with respect to two steady-state signals u_{ss1}, u_{ss2} are recorded through experimental tests. The process gain K_p can be determined as the following equation.

$$K_p = \frac{\Delta y}{\Delta u} = \frac{y_{ss2} - y_{ss1}}{u_{ss2} - u_{ss1}} \quad (2)$$

From the step response graph, the process dead time θ_p is defined as the time period between the beginning when the system is excited by a step input and the time when the state transition of the system is initialized. With this definition, the dead time can be estimated visually by one when conducting the experimental tests or calculated by using the intercept of the tangent line with the horizontal axis.

After determining parameters K_p and θ_p , **Equation (1)** can be rewritten in form of:

$$y(t) = \left(1 - e^{-\frac{t-\theta_p}{\tau_p}}\right) K_p \Delta u \quad (3)$$

By shifting the time origin of the step response to an amount that equals the dead time, the dead time θ_p , which is the alternative time origin, can be neglected in **Equation (1)** ($\theta_p = 0$). Hence, at the time $t = \tau_p$, the airflow output of the DAPP system is calculated as

$$y(\tau_p) = (1 - e^{-1}) \Delta y \approx 0.632 \Delta y \quad (4)$$

According to **Equation (4)**, by identifying the time $t_{0.632}$ when the airflow output reaches 63.2% of the steady state output value y_{ss} , the time constant is derived by the difference $t_{0.632} - \theta_p$.

The whole identification process is summarized in form of a pseudo-code algorithm and shown in **Table 1**.

Table 1: Pseudo-code algorithm for FOPDT model identification

Pseudo-code algorithm for FOPDT model identification
1. Find $\Delta u, \Delta y$ from the step response.
2. Calculate the process gain $K_p = \frac{\Delta y}{\Delta u}$.
3. Determine the dead time θ_p from the output response.
4. Calculate $63.2\% \Delta y$ from the step response.
5. Determine the response duration $t_{0.632}$. Calculate the time constant $\tau_p = t_{0.632} - \theta_p$.

4. Experimental tests



Figure 2: The two double-acting pistons pump in experimental tests.

The aim of this section is to provide experimental features of the tests which are conducted for collecting input-output data from the DAPP system. Furthermore, the model identification process of the DAPP system with the collected data is presented. And at the end of this section, the results and validation of the identified model are illustrated and discussed.

4.1 Experiment specifications

In order to produce calculation and model estimation of the DAPP system by the graphical method, the step response graph must be established. This can be accomplished by recording data of the step input signals and the airflow response signals. Exciting the DAPP system with different voltages input, the corresponding output data is recorded by the mass flow sensor mentioned in **Section 2**. The voltage excitation of the DAPP system is conducted 10 times with 10 distinct voltage values in form of pulse width modulation (PWM) pulses ranging from 10% to 55% duty cycle. The retrieved data is then divided into 2 groups; the first group of data is used for the purpose of model identification, and the other is served as validation data for the recently identified model. Moreover, to ensure the new steady state is achieved after the excitation, each scenario has a duration of 5 seconds and the sampling time is 10 milliseconds (ms).

4.2 Identification process

After the previous sub-section, groups of data are achieved and will be used for identifying the parameters of the FOPDT model in this subsection. The first parameter in the FOPDT equation that

needs to be determined is the dead time θ_p . According to the graphical method, this parameter is defined as the intercept of the tangent to the step response that has the largest slope with respect to the horizontal axis. In order to accomplish that, the line equation of the tangent to the step response must be established as the highest priority. Then, by generating data from each scenario of input in the 1st group through that equation, the tangent with the largest slope is found and the corresponding dead time is determined. The process gain is calculated from the step response in each scenario according to Equation (2). Following the algorithm in Table 1, the time constant can also be estimated. Finally, a comparative evaluation of each parameter among scenarios in the 1st group is carried out and the FOPDT model of the pump system is fully identified.

4.3 Results and validation

The entire experimental tests and the calculated parameters in each scenario are also included in Table 2.

Table 2: Results of experimental tests

Test No.	Δu (%)	Δy (ml/s)	K_p	θ_p (s)	τ_p
1	10	173	347	0.04	0.03
2	15	344	459	0.04	0.03
3	20	521	521	0.04	0.03
4	25	681	545	0.04	0.03
5	30	818	545	0.04	0.026
6	35	961	549	0.04	0.026
7	40	1041	520	0.04	0.03
8	45	1149	511	0.04	0.03
9	50	1348	539	0.04	0.033
10	55	1476	537	0.04	0.03

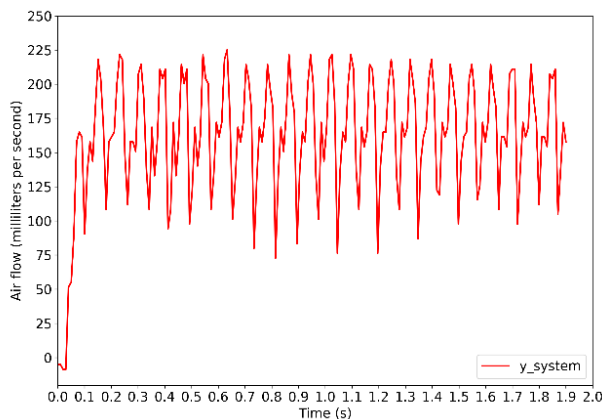


Figure 3: Output response in the 1st test scenario

For a full explanation of the above table, a brief view of the step response graph is indeed needed. Figure 3 shows the output response curve and the corresponding step input which belong to

the 1st test scenario. It can be seen from the figure that the system took a small period of time to start the state transition. This amount of time results from the inertia relying on the pump system itself which prevents the system from responding to the input voltage signal immediately. By this means, the dead time θ_p acts the same way as the delay time in Figure 3. As consequently, it can be estimated as 0.04 seconds.

After the derivation of the dead time, the time constant is computed by following the algorithm in Table 1. Hence, $\tau = t_{0.632} - \theta_p \approx 0.07 - 0.04 = 0.03$ (s).

As can be seen from Table 2, the parameters τ_p among the scenarios oscillate around an equilibrium point (≈ 0.03 seconds) and the dead time θ_p remains constant as 0.04 seconds throughout every scenario. On the other hand, the process gain K_p tends to change its value in low levels of airflow (< 500 ml/s) due to the nonlinear characteristics of the DAPP at a low level of airflow. When the BLDC motor reaches the high level of duty cycle ($> 20\%$), where the high level of airflow (> 500 ml/s) is generated by the DAPP. The gain K_p starts to fluctuate between 511 and 549 with a mean value of about 533. This means that the DAPP system has linear characteristics in a high level of airflow. Therefore, the FOPDT model will be used for designing the controller of the DAPP system in high levels of airflow (> 500 ml/s). The final FOPDT model is derived as follows, after extracting the mean value from each parameter.

$$\dot{y}(t) = -\frac{1}{0.03}y(t) + \frac{533}{0.03}u(t - 0.04) \tag{5}$$

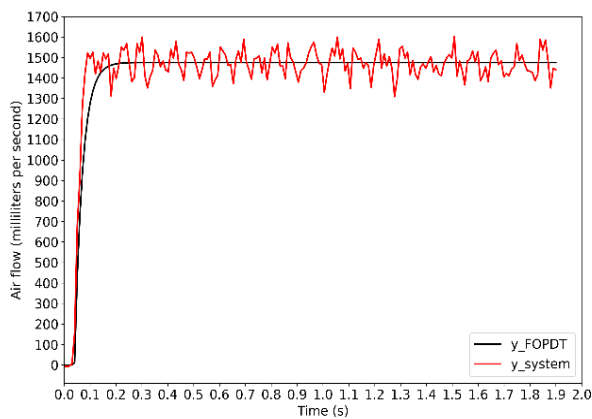
For the objectives of validation, the mean squared error (MSE) is used to evaluate the estimated model's performance. The equation of MSE is defined as

$$MSE_r = \frac{\sum |\hat{y}_{ss}(i) - y_{ss}(i)|^2}{\sum y_{ss}^2(i)} \tag{6}$$

where \hat{y}_{ss} is the steady state output airflow of the estimated FOPDT model in Equation (5); y_{ss} is the steady state output airflow of the DAPP system that is measured by the mass flow sensor, i denotes the number of samples in steady state in the r^{th} scenario. The MSE score of the FOPDT model with the 2nd group of data is summarized in Table 3 below. Figure 4 below shows the comparative evaluation between the output airflow of the estimated FOPDT model and the airflow measured by the sensor in 10th scenario.

Table 3: MSE scores of the FOPDT model with the 2nd group of data

Test No.	MSE
1	0.004479545
2	0.004493375
3	0.003943517
4	0.002815366
5	0.002896781
6	0.005190154
7	0.00262155
8	0.001692255

**Figure 4:** Comparison of output airflow in 10th scenario

From **Figure 4**, one restriction of the FOPDT model could be pointed out, that is the estimated output values do not fit well with fluctuation in steady-state. This disadvantage could be troublesome when designing an airflow controller that requires high accuracy because some peak values might do harm to the system itself. Alternatively, using a model with higher order or applying another identification method is one of the solutions. However, with the objective of controlling the volume that is pumped into the patient's lung, this estimated FOPDT model can be useful. In future work, research and studies on the volume controller based on this estimated FOPDT model will be conducted. Tuning the model parameter is also a branch to be concerned.

4. Conclusion

This paper presented an alternative method of system identification for medical ventilators. The FOPDT model was described and an algorithm was established to determine the parameters. The estimated model was then validated with the aspect of performance in the approximation system. Some restrictions of the model also are discussed. In future work, the volume parameters of the DAPP are going to be experimentally performed with the

prosthetic lung and the change in output impedance (change in the internal resistance of the prosthetic lung). In addition, the intelligent controller is applied for DAPP to observe and update the coefficients to ensure in two situations: the volume is constant or the volume changes based on the impedance change of the prosthetic lung.

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Author Contributions

Conceptualization, D. K. Nguyen and C. T. Truong; Methodology, D. K. Nguyen and C. T. Truong; Software, D. K. Nguyen; Validation, D. K. Nguyen and T. T. Nguyen; Formal Analysis, C. T. Truong; Investigation, T. T. Nguyen; Resources, C. T. Truong; Data Curation, D. K. Nguyen; Writing—Original Draft Preparation, D. K. Nguyen and C. T. Truong; Writing—Review & Editing, V. T. Duong; Visualization, D. K. Nguyen and C. T. Truong; Supervision, V. T. Duong; Project Administration, H. H. Nguyen; Funding Acquisition, T. T. Nguyen.

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